



**Solve linear  
equation**

A system of linear equations is a set of  $n$  linear equations in which each equation contains up to  $n$  variables or 'unknowns'. A simple example might be to find  $x$  and  $y$  given:

$$2x + 3y - 3 = 0$$

$$3x + 2y - 5 = 0$$

Open excel work sheet and insert the data as shown below:

5	A	B	C	D
6	Variables	Guess	Equations	squares
7	x	0	-3	9
8	y	0	-5	25
9			sum=	34
10				

$$C7=2*B7+3*B8-3$$

$$C8=3*B7+2*B8-5$$

$$D7=C7^2$$

$$D8=C8^2$$


$$D9=\text{SUM}(D7:D8)$$

D9     $f_x$     =SUM(D7:D8)


	A	B	C	D	E	F
1	System of Linear Equations					
2						
3						
4						
5						
6	Variables	Guess	Equations	squares		
7	x	0	-3	9		
8	y	0	-5	25		
9			sum=	34		
10						
11	<b>Solver Parameters</b> <span>✕</span>					
12	Set Target Cell:		\$D\$9		<span>📄</span>	
13	Equal To:		<input type="radio"/> Max <input type="radio"/> Min <input checked="" type="radio"/> Value of:		0	
14	By Changing Variable Cells:					
15	\$B\$7:\$B\$8		<span>📄</span>		<span>Guess</span>	
16	Subject to the Constraints:					
17			<span>Add</span>		<span>Options</span>	
18			<span>Change</span>		<span>Reset All</span>	
19			<span>Delete</span>		<span>Help</span>	
20						
21						
22						

1    2    3

Click

C14 

	A	B	C	D	E
1	<b>System of Linear Equations</b>				
2					
3					
4					
5					
6	<b>Vaiables</b>	<b>Guess</b>	<b>Equations</b>	<b>squares</b>	
7	<b>x</b>	<b>1.8</b>	<b>-5.77E-07</b>	<b>3.33E-13</b>	
8	<b>y</b>	<b>-0.2</b>	<b>-5.887E-07</b>	<b>3.47E-13</b>	
9			<b>sum=</b>	<b>6.8E-13</b>	
10					
11					
12					
13					
14					
15					
16					
17					
18					
19					

**Solver Results** 

Solver found a solution. All constraints and optimality conditions are satisfied.

☒ Keep Solver Solution  
☐ Restore Original Values

OK Cancel Save Scenario... Help

Reports

Answer  
Sensitivity  
Limits

H.W. Solve the following system equation using **Solver** function.

$$2x + 4y + 5z - 33 = 0$$

$$6x + 6y + 7z - 70 = 0$$

$$3x - 6y + 4z + 71 = 0$$

# **Non - linear Simultaneous Equations Solver**

Non-linear systems of equations are far more difficult to solve with paper and pencil, requiring a knowledge of calculus. Let's see if Solver is capable of coming to our aid. We will solve the nonlinear simultaneous equations:

$$x^2 + 2y^2 - 22.0 = 0$$

$$-2x^2 + xy - 3y + 11.0 = 0$$

	A	B	C	D	E
1	System of Non-linear Equations				
2					
3	$x^2 + 2y^2 - 22.0 = 0$				
4	$-2x^2 + xy - 3y + 11.0 = 0$				
5					
6					
7	<b>Variables</b>	<b>Guess</b>	<b>equations</b>	<b>square</b>	
8	<b>x</b>	<b>0</b>	<b>-22</b>	<b>484</b>	
9	<b>y</b>	<b>0</b>	<b>11</b>	<b>121</b>	
10			<b>sum=</b>	<b>605</b>	

$$C8=1*B8^2+2*B9^2-22$$

$$C9=-2*B8^2+B8*B9-3*B9+11$$

$$D8=C8^2$$

$$D9=C9^2$$


$$D10=SUM(D8:D9)$$

# System of Non-linear Equations


$$x^2 + 2y^2 - 22.0 = 0$$
$$-2x^2 + xy - 3y + 11.0 = 0$$

Variables	Guess	equations	square
x	0	-22	484
y	0	11	121
		sum=	605

**Solver Parameters**

Set Target Cell:  

Equal To: ☐ Max ☐ Min ☒ Value of:

By Changing Cells:  

Subject to the Constraints:

Click

	A	B	C	D	E	F
1	System of Non-linear Equations					
2						
3	$x^2 + 2y^2 - 22.0 = 0$					
4	$-2x^2 + xy - 3y + 11.0 = 0$					
5						
6						
7	Variables	Guess	equations	square		
8	x	-0.276	-5.7E-06	3E-11		
9	y	3.311	-4.2E-05	2E-09		
10			sum=	2E-09		
11						
12						
13						
14						
15						
16						
17						
18						
19						
20						
21						

Solver Results

Solver found a solution. All constraints and optimality conditions are satisfied.

☒ Keep Solver Solution  
☐ Restore Original Values

Reports

Answer  
 Sensitivity  
 Limits

With starting values of 1 for both variables Solver suggests an approximate solution with  $x = 1.99994$  and  $y = 3.00004$ . The function evaluate to values somewhat larger than 0. Experimentation shows  $x = 2$  and  $y = 4$  is an exact solution. Of course, since the equations contain 2 and?, **multiple solutions are possible. Starting with 0 for each variable, Solver reported  $x = 0.2763$  and  $y = 3.3109$  as a solution.**

**H.W. : Try that with starting with guess values of 1,1**