

**Control objective :**

- 1) Safety
- 2) Environmental protection
- 3) Operational constraints
  - a) Equipment protection
  - b) Smooth operation
- 4) Product quality
- 5) Profit
- 6) Monitoring and diagnosis

**Process dynamic:**

Refers to the time-varying behavior of controlled or uncontrolled process behavior when there are subject to disturbances.

**Process control:**

Controlling the unsteady state behavior and bring the system back to the steady – state.

**Classes of variables:**

- 1) Un controllable variables: ambient condition ,catalyst activity.
- 2) Controllable variables: temperature ,pressure ,flow ,level ,pH.
- 3) Product variables: color ,viscosity, composition.

**Laplace transformation:**

Laplace transform is useful for providing qualitative analysis of dynamic processes. Laplace transform is an operator that transforms the independent variable of a function from the time domain to the s-domain. In this case, it facilitates the solution of linear differential equation as Laplace transform converts the ODE into algebraic variables.

**Definition of the Laplace transformation:**

$$f(s) = \int_0^{\infty} f(t)e^{-st} dt$$

$s$  is variable defined in the complex plane (i.e. , $s=a+jb$ )

### Transformation of simple functions:

#### 1) Exponential function

$$f(t) = e^{-at} \quad \text{for } t \geq 0$$

Then

$$\mathcal{L}[e^{-at}] = \frac{1}{s+a}$$

#### 2) The step function

$$f(t) = \begin{cases} 0 & t < 0 \\ A & t > 0 \end{cases}$$

#### 3) Ramp function

$$f(t) = at \quad \text{for } t \geq 0 \text{ with } a \text{ is constant}$$

$$\text{Then } \mathcal{L}[at] = \frac{a}{s^2}$$

#### 4) Trigonometric function

$$f(t) = \sin \omega t$$

$$\mathcal{L}[\sin \omega t] = \frac{\omega}{s^2 + \omega^2}$$

$$f(t) = \cos \omega t$$

$$\mathcal{L}[\cos \omega t] = \frac{s}{s^2 + \omega^2}$$

#### 5) Derivatives

$$\left[ \frac{d^n f(t)}{dt^n} \right] = s^n f(s) - s^{n-1} f(0) - s^{n-2} f'(0) \dots - s f^{(n-2)}(0) - f^{(n-1)}(0)$$

$$\mathcal{L}\left[ \frac{df(t)}{dt} \right] = s f(s) - f(0)$$

$$\mathcal{L}\left[ \frac{d^2 f(t)}{dt^2} \right] = s^2 f(s) - s f(0) - f'(0)$$

## 6) Integrals

$$\mathcal{L}\left[\int_0^t f(t)dt\right] = \frac{1}{s}f(s)$$

**Final –value theorem:**

$$\lim_{t \rightarrow \infty} f(t) = \lim_{s \rightarrow 0} [sf(s)]$$

**Initial-value theorem**

$$\lim_{t \rightarrow 0} f(t) = \lim_{s \rightarrow \infty} [sf(s)]$$