

Routh stability analysis

The characteristics equation is:

$$p(s) = a_n s^n + a_{n-1} s^{n-1} + \dots + a_1 s + a_0 = 0$$

Then construct the following matrix from the coefficient of characteristics equation and contain n+1 of rows:

$$\begin{array}{cccc} 1 & a_n & a_{n-2} & a_{n-4} \\ 2 & a_{n-1} & a_{n-3} & a_{n-5} \\ 3 & G_1 & G_2 & G_3 \\ 4 & F_1 & F_2 & F_3 \\ \vdots & \vdots & \vdots & \vdots \\ n+1 & N_1 & N_2 & N_1 \end{array}$$

$$G_1 = \frac{a_{n-1} \cdot a_{n-2} - a_n \cdot a_{n-3}}{a_{n-1}}$$

$$G_2 = \frac{a_{n-1} \cdot a_{n-4} - a_n \cdot a_{n-5}}{a_{n-1}}$$

$$F_1 = \frac{G_1 \cdot a_{n-3} - a_{n-1} \cdot G_2}{G_1}$$

$$F_2 = \frac{G_1 \cdot a_{n-5} - a_{n-1} \cdot G_3}{G_1}$$

We select the first column and if all elements of this column is positive and no change of sign then the system is stable.

If change of sign of this column then the system is unstable.