**جامعة تكريت**

**كلية الهندسة**

**قسم الهندسة الميكانيكية**

**ديناميك حرارة 1 الكورس االول اعداد**

 **الدكتور المهندس**

**حميد جاسم خلف األحبابي**

# **Thermodynamics** − **Lectures**

**By**

**Dr.Hameed Jassim Khalaf**

**الجامعة : تكريت الكلية : الهندسة القسم العلمي : الهندسة الميكانيكية أسم / رمز المقرر : ديناميك حرارة /ه .م 232 عدد الساعات/اسبوع : 3)2نظري1+ صف تدريب class Tutorial) تاريخ االعداد : 2022/10/1**

 **الكورس االول – ديناميك حرارة 1**





**الكتاب المنهجي :**

**-Applied Thermodynamics for Engineering Technologists, Third edition مكتبة التعليم المجاني-قسم الميكانيك EASTOP.D.T by,**

**الكتاب المصدري:**

 **-Thermodynamics : An Engineering Approach, by Yunus A.Gengel**

#### **Chapter One**

#### **Basic Concepts Related To Thermodynamics**

#### **1.1 Introduction**

Thermodynamics, like other physical sciences, is based on observation of nature.

- **The first law of thermodynamics**: is simply an expression of the conservation of energy principle, and asserts that energy is a thermodynamic property.

- **The second law of thermodynamics**: asserts that energy has quality as well as quantity, and actual processes occur in the direction of decreasing quality of energy.

- The term *thermodynamics* was first used in publication of Lord Kelvin in 1849.

- The first thermodynamic text book was written in 1859 by William Rankine a professor at the University of Glasgow.

### **1.2 Definition of Engineering Thermodynamics**

 Thermodynamic can be defined as the science of energy. The name thermodynamics stems from the Greek words **thermos** (heat) and **dynamics** (power).

#### **Thermodynamics (Greek word)** →

Today the same name is widely taken to include all parts of :

Energy and energy transformations, including power production, refrigeration, and relationships between the properties of matter.

 Engineering thermodynamics is the subject that deals with the study of the science of thermodynamics and the usefulness of this science in the engineering design of processes, devices, and system involving the effective utilization of energy and matter for the benefit of humankind.

### **1.3 Applications of Engineering Thermodynamics**

Some examples: electric , heating and air-conditioning systems, the refrigerator, the humidifiers, the pressure cooker, the water heater, the shower, the iron, the computer, the TV,

Engines,….etc.

#### **1.4 Definition of thermodynamics**

Thermodynamics may be defined as follows:

*Thermodynamics is a clear science which deals with the relations between heat, work and properties of system which are in equilibrium. It describes state and change in state of physical system.*

Thermodynamics is *the science that deals with the interaction between energy and material systems.*

Thermodynamics, basically includes four laws: Zeroth, First, Second and Third law of thermodynamics.

• The *First law* throws light on concept of internal energy

**القانون االول يلقي الضوء على الطاقة الداخلية**

• The *Zeroth law* deals with thermal equilibrium and establishes a concept of temperature

**يتعامل القانون الصفري مع التوازن الحراري ويؤسس مفهوم درجة الحرارة**

• The *Second law* indicates the limit of converting heat into work and introduces the principle of increase of entropy.

```
يشير القانون الثاني الى حد تحويل الحرارة الى عمل ويقدم مبدأ زيادة األنتروبيا
```
The *Third law* defines the absolute zero entropy.

**يحدد القانون الثالث أنتروبيا الصفر المطلق** These laws are based on experimental observations and have no mathematical proof. Like all physical laws, these laws are based on logical reasoning.

```
تسستند هذه القوانيين الى المالحظات التجريبية وليس لها دليل رياضي، مثل جميع القوانيين 
                         الفيزيائية تستند هذه القوانيين الى التفكير المنطقي.
```
#### **1.5 Thermodynamic system**

1.5.1 System, Boundary, and Surroundings

System, A system is a finite quantity of matter or a given region of space choose of study (Fig.1.1).



Fig. 1.1 The system

 Boundary, The actual or hypothetical envelope enclosing the system is the boundary of the system. The boundary may be fixed or it may be move, as and when a system containing a gas is compressed or expanded. The boundary may be real or imaginary.

Surroundings, is those things outside the system.

#### **1.5.2 Closed system**

In system in which mass does not cross the system boundary, but energy may cross the system boundary (Fig.1.2). Closed system is also known as control mass.



Fig. 1.2 Closed system

## **1.5.3 Open system**

Any system in which both mass and energy may cross the system boundary (Fig.1.3).



Fig. 1.3 Open system

#### **1.5.4 Control volume and Control surface**

Some author call an open system a control volume and its boundary a control surface.

1.5.5 Non-flow and flow processes

The processes undergone by the fluid in a closed system are described as non-flow processes, whereas those undergone by the fluid in an open system are referred to as flow processes.

#### **1.5.6 Isolated system**

Any system in which neither mass nor energy crosses the system boundary (Fig. 1.4).



Fig. 1.5 Isolated system

### **1.5.7 Adiabatic system**

 A system which thermally insulated from its surroundings is called an adiabatic system. It can, exchange work with its surroundings . If it does not, it becomes an isolated system.

#### **1.6 Macroscopic and Microscopic**

System can be studied from macroscopic or a microscopic point of view.

Macroscopic approach : the macroscopic approach to thermodynamics is concerned with the gross or overall behavior. This sometimes called classical thermodynamics.

Microscopic approach: the microscopic approach to thermodynamics, known as statistical thermodynamics is concerned directly with the stricter of matter.

#### **1.6.1 Macroscopic system analysis**

 The analysis of the systems at the continuum level (i.e molecular dimensions and time scales do not enter into the analysis ). This is the domain of classical and non-equilibrium thermodynamics.

#### **1.6.2 Microscopic system analysis**

 The analysis of the systems at the atomic level. This is the domain of statistical thermodynamics.

#### **1.7 Thermodynamic equilibrium**

A system is in *thermodynamic equilibrium* if the temperature and pressure at all points are same.

 1. Thermal equilibrium : the temperature of the system does not change with time and has same value at all points of the system.

 2. mechanical equilibrium : there are no unbalanced forces within the system or between the surroundings. The pressure in the system is same at all points and does not change with respect to time.

 3. chemical equilibrium : no chemical reaction takes place in the system and the chemical composition which is same throughout the system does not vary with time.

#### **1.8 Properties of systems**

 A property of a system is a characteristic of the system which depends upon its state, but not upon how the state is reached. There are two types of property :

 1. Intensive properties : these properties do not depend on the mass of the system. Examples, Temperature and pressure.

 2. Extensive properties : these properties depend on the mass of the system . Example. Volume . Extensive properties are often divided by mass associated with them to obtain the intensive properties. For example, if the volume of the system of mass m is V , then the specific volume of matter within the system is  $\frac{v}{m} = v$ , which is an intensive property.

#### **1.9 State**

State : is the condition of the system at an instant of time as described or measured by its properties. All properties are state or point functions.

#### **1.10 Process**

A process occurs when the system undergoes a change in a state or an energy transfer at a steady state.

A process may be :

 1. non-flow process : in which a fixed mass(i.e closed system) within the defined boundary is undergoing a change in state. Example : a substance which is being heated in a closed cylinder undergoes a non-flow process.

 2. flow process : in which mass is entering and leaving through the boundary of an open system .

### **1.11 Cycle**

Any process or series of processes whose end states are identical is termed a cycle.



Fig. 1.5. Cycle in operations.

#### **1.12. Point Function**

When two properties locate a point on the graph, (coordinate axes) then those properties are called as point function.

Examples, pressure, temperature, volume , etc.

$$
\int_{V_1}^{V_2} dV = V_2 - V_1 \quad (an exact differential)
$$

#### **1.13 Path Function**

There are certain quantities which cannot be located on the graph by a point but are given by the area or so, on that graph. In that case, the area on the graph , related to the particular process, is a function of the path of the process. Such quantities are called **path functions**.

Examples, Heat , Work, etc.

Heat and work are *inexact differentials.* Their change cannot be written as difference between their end states.

Thus  $10<sub>2</sub>$  or  $O<sub>1-2</sub>$ 

 $\int_1^2 \delta W \neq W_2 - W_1$  and is shown as  ${}_1\mathrm{W}_2$  or  $\mathrm{W}_{1\text{-}2}$ Similarly  $\int_1^2$ 

**Note:**

The operator

δ is used to denote inexact differentials and operator d is used to denote exact differential

## **1.14 Temperature**

-The temperature is a thermal state of a body which distinguishes a hot body from a cold body.

-The temperature of a body is proportional to the stored molecular energy.

- A particular molecule does not have a temperature, it has energy

**مالحظة: الجزيئة ليس لديها درجة حرارة ، تمتلك طاقة - النظام له درجة حرارة اما جزيئة معينة داخل النظام ليس لديها درجة حرارة لديها طاقة حركية.**

- The gas as a system has a temperature. **حرارة درجة لديه النظام مثل الغاز -**

-Instruments for measuring ordinary temperatures are known as *thermometers* and those for measuring high temperatures are known as *pyrometers.*

**-**It has been found that a gas will note occupy any volume at a **certain temperature**. This temperature is known as *absolute zero temperature.*

**لقد وجد أن الغاز لن يشغل أي حجم عند درجة حرارة معينة،وتعرف درجة الحرارة هذه باسم درجة حرارة الصفر المطلق** 

-The point of absolute zero temperature is found to occur at 273 ∙ 15℃ **below** the freezing point of water. Then

Absolute temperature = Thermometer reading in  $°C + 273$ 

Absolute temperature can also be represented in degree Kelvin denoted by K (SI unit).

## **1.15 Zeroth Law of Thermodynamics**

-*Zeroth Law of Thermodynamics*: states that if two systems are each equal in temperature to a third, they are equal in temperature to each other.

## **1.16 Pressure**

1.16.1 **Definition of pressure**

Pressure is define as a force per unit area. Pressures are exerted by gasses, vapors and liquids.

جهاز قياس الضغط يسجل الفرق بين ضغطين وهذا الفرق بين الضغط المسلط من قبل المائع والضغط الجوي ambient atmospheric pressure . وتلك الجهاز يستدل على الضغط اما فوق الضغط الجوي او اقل من الضغط الجوي ، اما الفوق الضغط الجوي يسمى ضغط المقياس pressure gauge واالقل من الضغط الجوي . vacuum pressure ويسمى negative pressure سالب يكون A schematic diagram showing the gauge pressure pressure, vacuum pressure and the absolute pressure is given in Fig.1.6.

**Gauge pressure:** the pressure which is above the atmospheric pressure is known as gauge pressure; the atmospheric pressure is zero gauge pressure.(Fig.1.6)

**Vacuum pressure:** the pressure which is below the atmospheric pressure is known as a vacuum pressure.(Fig.1.6)



Fig.1.6. Schematic diagram showing gauge, vacuum and absolute pressures.

Mathematically:

(i) Absolute pressure= Atmospheric pressure + Gauge pressure

$$
P_{abs} = P_{atm} + P_{gauge}
$$

(ii) Vacuum pressure = Atmospheric pressure – Absolute pressure

Note:

Vacuum is defined as the absence of pressure. A perfect vacuum is obtained when absolute pressure is zero, at this instant molecular momentum is zero.

Atmospheric pressure is measured with the help of barometer.

**Manometer:** it is a device which measures either gauge pressure or vacuum pressure.

**Barometer**: the atmospheric pressure is measured by a device called a barometer.

# 1.16.2 **Unit of pressure**

1. The fundamental SI unit in N/m<sup>2</sup> (sometimes called *Pascal*, Pa)

- 2. Pressure is also measured in bar,  $1bar = 10^5$  N/m<sup>2</sup>
- 3. Standard atmospheric pressure  $= 1.01325$  bar  $= 0.76$  m Hg( or 760 mmHg).

The pressure unit Pascal is too small for pressure; therefore kilopascal, Mega Pascal and bar commonly used.

 $1 \text{ kPa} = 10^3 \text{ Pa}$ 

 $1 \text{ MPa} = 10^6 \text{ Pa} = 10^3 \text{ kPa}$ 

 $1 \text{ bar} = 10^5 \text{ Pa} = 100 \text{ kPa}$ 

Atmospheric pressure varies with location on the earth, a standard reference can be defined and used to express other pressures

1 standard atmosphere (atm.) =101.325 Pa

 $=101.325$  kPa

 $=1.01325$  bar

Absolute pressure = atmospheric pressure  $\pm$  Gauge pressure

Or, 
$$
p_{abs} = p_a + p_{gauge}
$$

 $p_{gauge} = \rho gh$ 

Where,

 $\rho = density$  ;  $g = acceleration = 9.81 \, m/s^2$  ;

 $h = high of liquid column$ 

Analysis

Using the relation

 $p = \rho gh$ 

Let p=1 bar=10<sup>5</sup> N/m<sup>2</sup> ;  $\rho =$ 1000  $kg/m^3$  for water ;  $g = 9.81 m/s^2$ 

For water

$$
1 \times 10^5 = 1000 \times 9.81 \times h
$$
  

$$
h = \frac{1 \times 10^5}{1000 \times 9.81} = 10.2 \text{ m of water}
$$
  
or 1 mm of water =  $9.81 \frac{N}{m^2}$  = 9.81 Pa

By using the relation

$$
h_{water} \times S_{water} = h_{mercury} \times 13 \cdot 6
$$

Therefore, 1 bar =  $750$  mm of Hg

## 1.16.3 U-tube manometer

Low pressures are generally determined by manometers which employ liquid columns. A U-tube manometer is in the form of U-tube and is made of glass (Fig.1.7).



Fig.1.7. Principle of U-tube manometer.

Considering equilibrium condition, we have

 $p_{atm} + w_a h_a = p_i + w_i h_i$ 

Where,  $p_{atm} = Atmospheric pressure$ 

 $p_i$  = Pressure over water surface in the container

 $h_a$  = Heigh of liquid in  $U$  – tube manometer

$$
h_i =
$$

Difference between water surface and lower surface of the liquid in manometer  $w_a = Specific weight of liquid$ 

 $w_i = Specific weight of water$ 

1.17 Specific volume

The specific volume of a system is the volume occupied by the unit mass

Specific volume  $= v =$ Total Volume mass = V  $\dot{m}$  $(m^3/kg)$ 

**Example 1.1.** *Convert the following readings of pressure to kPa assuming that barometer read 760 mm of Hg.*

**مالحظة: الباروميتر (barometer) جهاز لقياس الضغط الجوي** 

(i) 80 cm of Hg

(ii) 30 cm Hg vacuum

(iii)  $1.35 \text{ m H}_2\text{O}$  gauge

(iv) 4.2 bar

**Solution.** Assuming density of Hg

 $\rho_{Hg} = 13600 \ kg/m^3$ 

Where  $\rho_{hg} = density of Hg$ 

Pressure of 760 mm of Hg will be

$$
p = \rho_{Hg}gh = 13600 \times 9 \cdot 81 \times \frac{760}{1000} \approx 101 \cdot 325 \, kPa
$$

### i.e **760 mm of Hg =101.325 kPa**

## **(i) pressure of 80 cm of Hg**



800 p

$$
p = \frac{101 \cdot 325 \times 800}{760} = 106 \cdot 65 \, kPa \quad (Ans.)
$$

**(ii) 30 cm Hg vacuum**

$$
= 76 - 30 = 46 \text{ cm of Hg absolute}
$$

$$
= \frac{101 \cdot 325 \times 460}{760} = 61 \cdot 328 \text{ kPa} \quad (Ans \cdot)
$$

**(iii) pressure due to 1.35 m H2O gauge**

$$
p = \rho_{H_2O} \times g \times h = 1000 \times 9.81 \times 1.35 = 13.238 \, kPa \, (Ans.)
$$

**(iv) 4.2 bar**

$$
= 4 \cdot 2 \times 10^5 = 420000 Pa = \frac{420000}{10^3} = 420 kPa \quad (Ans \cdot)
$$

**Note.**

Pressure of 1 atmospheric = 760 mm of Hg =  $101325$  N/m<sup>2</sup>

**Example 1.2.** *On a piston of 10 cm diameter a force of 1000 N is uniformly applied .Find the pressure on the piston.*

**Solution**. Diameter of the piston, d=10 cm=0.1 m

∴ Pressure on the piston

$$
p = \frac{Force}{Area} = \frac{F}{A} = \frac{F}{\pi d^2 / 4} = \frac{1000}{\pi (0.1)^2 / 4} = 127307 \ N/m^2 = 127 \cdot 307 \ kN/m^2
$$

**Example 1.3.** *A tube contains an oil of specific gravity 0.9 to a depth of 120 cm. Find the gauge pressure at this depth* (*in kN/m<sup>2</sup>*).

Solution.

Specific gravity of oil  $=0.9$ 

Depth of oil in the tube, h=120 cm=1,2 m

We know that

 $p = \rho gh$   $\rho = density \, in \, kg/m^3$ 

Specific gravity =  $S = \frac{density~of~matter}{density~of~matter}$ density of matter  $=\frac{\rho_{matter}}{\rho_{water}}$  $\rho_{water}$ 

In this example the matter is the oil, hence

 $\rho_{oil} = S \times \rho_w = 0.9 \times 1000$ 

 $p = (0.9 \times 100) \times g \times h = (0.9 \times 1000) \times 9.81 \times 1.2 = 10.595 kN/m^2$ 

**Example 1.4.** *A U-tube manometer is connected to a gas pipe. The level of the liquid in the manometer arm open to the atmosphere is 170 mm lower than the level of the liquid in the arm connected to the gas pipe. The liquid in the manometer has specific gravity of 0.8. find the absolute pressure of the gas if the manometer reads*

*760 mmHg.*



Fig.1.8

## **Solution.**

Equating pressure on both arms above the line XX, Fig.1.8

 $p_{gauge} + p_{liquid} = p_{atm}$  (i) Now  $p_{liquid} = \rho gh = (0.8 \times 1000) \times 9.81 \times \frac{170}{1000}$  $\frac{170}{1000}$  = 1334.16  $N/m^2 = \frac{1334.16}{105}$  $/m^2 = \frac{1334.16}{10^5} = 0.0133416$  bar

Substituting these value in eqn.(i) above, we have

 $p_{gas} + 0.0133416 = 1.01325$ ∴  $p_{gas} = 1 \cdot 01325 - 0 \cdot 0133416 = 0 \cdot 9999$  *bar* (*Ans* ·)

## **1.17. Reversible and Irreversible Processes**

**Reversible process:** *A reversible process (also sometimes known as quasi-static process) is one which can be stopped at any stage and reversed so that the system and surroundings are exactly restored to their initial states.*

**عملية قابلة للعكس )تعرف أحيانا باسم عملية شبه ثابتة (هي عملية يمكن أيقافها في أي مرحلة وعكسها بحيث يتم استعادة النظام والمناطق المحيطة به الى حالتها األولية**

**This process has the following** *characteristics:*

1.It must pass through the same states on the reversed path as were initially visited on the forward path.

االجراء يجب ان يمر عبر نفس الحاالت states على المسار المعكوس كما تم المرور عليه في البداية على المسار االمامي

2.It must pass through a continuous series of equilibrium states.

يجب ان يمر عبر سلسلة مستمرة من حاالت التوازن



**Fig.1.9 .Reversible process**

## **Examples. Some examples of nearly reversible processes are:**

- (i) Frictionless relative motion.
- (ii) Expansion and compression of spring
- (iii) Frictionless adiabatic expansion or compression of fluid.
- (iv) Polytropic expansion or compression of fluid.
- (v) Isothermal expansion or compression
- التحليل الكهربائي Electrolysis) vi(

**Irreversible process:** *An irreversible process is one in which heat is transferred through a finite temperature*.

**العملية التي ال رجعة فيها هي العملية التي تنتقل فيها الحرارة من خالل درجة حرارة محدودة**

## **Examples.**

(i)Relative motion with friction

(ii)Combustion

(iii)Diffustion

(iv)Free expansion

(v)Throttling

(vi) Electricity flow through a resistance

(vii)Heat transfer

(viii)Plastic deformation

 *An irreversible process is usually represented by a dotted(or discontinuous)line joining the end states to indicate that the intermediate states are indeterminate(Fig.1.10).*

**عادة ما يتم تمثيل عملية ال رجعة بخط منقط ينظم الى الحاالت النهائية لالشارة الى ن الحاالت الوسطية غير محددة**



**Fig.1.10.Irreversible process**

**Irreversibilities are of** *two types:*

**1. External irreversiblilities.** *These are associated with dissipating effects outside the working fluid.*

**هذه ترتبط بتأثيرات تبديد dissipating خارج مائع التشغيل)النظام(**

**2. Internal irreversibilities.** *These are associated with dissipating effects within the working fluid.*

**هذه ترتبط بتأثيرات تبديد داخل مائع التشغيل)النظام(**

## 1.18 **Energy, Work and Heat**

## **1.18.1. Energy**

Energy is a general term embracing energy in transition and stored energy.

**الطاقة مصطلح عام يشمل الطاقة التي تمر بمرحلة انتقالية والطاقة المخزنة**

The stored energy of a substance may be in the forms of *mechanical energy* and *internal energy* (other forms of stored energy may be chemical energy and electrical energy).

Part of the stored energy may take the form of either potential energy (due to high above a chosen datum line) or kinetic energy (due to velocity).

*in a non-flow process usually there is no change in potential or kinetic energy hence mechanical energy will not enter the calculations.*

*In a flow process, however, they may changes in both potential and kinetic energy and these must be taken into account.*

*Heat and work are the forms of energy in transition.*

**مالحظة : الطاقة عندما تنتقل )تعبر جدار النظام boundary system )يكون شكلها اما شغل او حرارة**

## **1.18.2 Work and Heat**

$$
Work = Force \times distance = F \times L
$$

**عادتا في ديناميك الحرارة يدرس النظام وللنظام جدار يسمى system of boundary وعندما يحدث لهذا الجدار ازاحة نتيجة القوة المسلطة عليه والناتجة عادتا من الضغط المسلط على جدران النظام وهذه االزاحة تكون باتجاة القوة المسلطة وكما موضح في الشكل )11-1()أ( والذي يوضح اسطوانة يتحرك داخلها مكبس piston وتسمى هذه المنظومة arrangement cylinder-piston وهو نفس ما موجود في محرك احتراق داخلي)محرك السيارة(، يسمى الشغل الناتج من االزاحة لجدران النظام work boundary ويكون موجب عندما تكون االزاحة موجبة) حالة التمدد) process expansion )وسالب عندما تكون االزاحة**  )**compression process( سالبة**



Fig.1.11

الشكل (a) النظام يسلط ضغط على المكبس ويحركه الى الاعلى وينتج تمدد في الحجم وبالتالي يكون الشغل موجب كونه مسلط من قبل النظام )خارج من النظام(

Sign convention:

(i) if the work is done by the system on the surroundings , the work is said to be positive

(ii) if the work is done on the system by the surroundings, the work is said to be negative.

الشكل)b )شغل ميكانيكي مصدره من الخارج surroundings مسلط على النظام ، الشغل في هذه الحالة يكون سالب

## **Heat**

Heat denoted by the symbol Q, may be, defined in an analogous way to work as follows:

*" Heat is 'something' which appears at the boundary when a system changes its state due to a difference in temperature between the system and its surroundings".*

 *Heat, like work, is a transient quantity*, which only appears at the boundary while a change is taking place within a system.

الشغل والحرارة ليس differentials exact وتكاملهما يجب ان يكون بهذه الصيغة:

 $\int_{1}^{2} \delta W = W_{1-2}$  0r  $\int_{1}^{2} \delta W = W_{1-2}$  Or  $_1$ W<sub>2</sub> (or W) and  $\int_{1}^{2} \delta Q = Q_{1-2}$  or  $\int_{1}^{2} \delta Q = Q_{1-2}$  or  $_1Q_2$  (or Q)

Sign convention :

(i) if the heat flows into a system from the surroundings, the quantity is said to be positive

(ii) if the heat flows from the system to the surrounding it is said to be negative.



Fig.1.12.Sign convention for work and heat

## **Comparison of Work and Heat**

#### *Similarities***:**

(i) Both are path functions and inexact differentials.

(ii) Both are boundary phenomenon i.e, both are recognized at the boundaries of the system as they cross them.

(iii) Both are associated with a process, not a state. Unlike properties , work and heat has no meaning at a state.

(iv) systems possess energy, but not work or heat.

**تمتلك األ نظمة الطاقة وال تمتلك شغل او حرارة**

Dissimilarities:

(i) In heat transfer temperature difference is required.

(ii) In a stable system there cannot be work transfer, however, there is no restriction for the transfer of heat.

**في نظام مستقر ال يمكن ان يكون هناك نقل شغل، ومع ذلك، ال توجد قيود على نقل الحرارة**

### **1.19 Reversible Work**

الشكل)(a(1.13 (افترضناه يحتوي على مائع مثالي بدون احتكاك اثناء الجريان ، والشكل عبارة عن مكبس يتحرك داخل اسطوانة من دون احتكاك (عملية ارجاعية reversible process) وتسمى ايضا frictionless process ، لتكن :



Fig.1.13(a)

A= Cross-sectional area of the piston,

P= pressure of the fluid at any instant,

dl= the distance moved by the piston under the action of the force exerted.

$$
p = \frac{F}{A} \quad or \quad F = pA
$$

Work done by the fluid= $(pA) \times dl = pdV$ 

Where  $dV = a$  small increase in volume, or considering unit mass

*Work done* = 
$$
pdv
$$

Where  $v = specific volume$ 

Note that specific volume  $=\frac{Total\ volume}{mass}$ mass

Or  $v = \frac{v}{m}$  $\frac{v}{m}$  :  $V = mv$  This is only true when

(a) the process is frictionless

(b) the different in pressure between the fluid( or system) and its surroundings during the process is infinitely small. Hence when a reversible process takes place between state 1 and state 2 , we have

work done by the unit mass of fluid = 
$$
\int_{1}^{2} pdv
$$

The work done by the fluid during any reversible process is therefore given by the area under the line of process plotted on a  $p - v$  diagram [Fig.1.13(b)].

i.e Work done = Shaded area on Fig 
$$
\cdot
$$
 14(b)

$$
=\int_1^2 p dv
$$



Fig.1.13 (b)

**Example 1.5. The properties of a closed system change following the relation**  between pressure and volume as  $pV = 3$  , where p is in bar V is in m $^3$ . **Calculate the work done when the pressure increases from 1.5 bar to 7.5 bar.**

**Solution.**

**Initial pressure,**  $p_1 = 1.5$  bar

**Finial pressure,**  $p_2 = 7.5$  bar

**Relation between p and V, pV=3.0**

**Work done, W=?**

**The work done during the process is given by**

$$
W=\int_{V_1}^{V_2} pdV
$$

From the above relation  $V_1 = \frac{3}{n}$  $\frac{3}{p_1} = \frac{3}{1}$  $\frac{3}{1.5}$  = 2 m<sup>3</sup>

$$
V_2 = \frac{3}{2} = \frac{3}{7.5} = 0 \cdot 4 \, m^3
$$

From the relation pv=3 , we find  $p=\frac{3}{\nu}$ V

$$
W = 10^5 \times \int_2^{0.4} \frac{3}{V} dV = 10^5 \times 3[LnV]_2^{0.4}
$$
  
= 10<sup>5</sup> × 3[Ln0.4 - Ln2]  
= -3 × 10<sup>5</sup> Ln( $\frac{2}{0.4}$ )  
= -3 × 10<sup>5</sup> Ln 5  
= -3 × 10<sup>5</sup> × 1.61  
= -4.83 × 10<sup>5</sup> Nm  
= -4.83 × 10<sup>5</sup> J = -4.83  $\frac{10^5}{10^3}$  = -4.83 × 10<sup>2</sup> kJ = -483 kJ (Ans.)

**Example 1.6. To a closed system 150 kJ of work is supplied. If the initial** *volume is*  $0 \cdot 6$   $m^3$  and pressure of the system changes as  $p = 8 - 4V$ , where **p is in bar and V is in m<sup>3</sup> , determine the final volume and pressure of the system.**

**Solution.**

**Amount of work supplied to a closed system = 150 kJ**

**Initial volume,**  $V_1 = 0.6$  **m<sup>3</sup>** 

**Pressure-volume relationship, p=8 – 4V**

**The work done during the process is given by**

**From the relation p=8-4V , substitute from p in this relation:**

$$
W=\int_{V_1}^{V_2} p dV=10^5 \int_{0.6}^{V_2} (8-4V) dV
$$

**10=bar 1 <sup>5</sup> 10 لتحويل الضغط من البار الى الباسكال حيث ان (Pa <sup>5</sup> مالحظة: ضرب التكامل اعاله في علما ان 1=Pa1 )**

$$
W=10^5[8V-4\frac{V^2}{2}]_{0.6}^{V_2}
$$

 $= 10^5 [8(V_2 - 0.6) - 2(V_2^2 - 0.6^2)]$  $= 10^5 [8V_{2}-4\cdot 8 - 2V_{2}^2+0\cdot 72]$  $= 10^5 [8V_2 - 2V_2^2 - 4 \cdot 08]$ 

But this work is equal to  $-150$ kJ, as this work is supplied to the system

Note: 
$$
1kJ = 10^3 J
$$
  
\n
$$
\therefore -150 \times 10^3 J = 10^5 [8V_2 - 2V_2^2 - 4 \cdot 08]
$$
\n
$$
-150 = 10^2 [8V_2 - 2V_2^2 - 4 \cdot 08]
$$
\nor 
$$
2V_2^2 - 8V_2 + 2 \cdot 58 = 0
$$

**الحل بطريقة الدستور اليجاد الحجم المطلوب**

$$
V_2=\frac{8\pm\sqrt{64-4\times2\times2\cdot58}}{4}
$$

$$
=\frac{8\pm 6\cdot 585}{4}=0\cdot 354\; m^3
$$

**اشارة الجمع تهمل في هذا المثال ، وضح لماذا ؟**

Final volume,  $V_2 = 0.354 m^3$  (Ans.<sup>.</sup>)

And, Final pressure,  $p_2 = 8 - 4V = 8 - 4 \times 0.354 = 6.584$  *bar* (*Ans*)

### **Reversible Work**

**Example 1.7. A fluid at a pressure of 3 bar, and with a specific volume of 0.18 m<sup>3</sup> /kg, contained in a cylinder behind a piston expands reversibly to a**  pressure of **o.6** bar according to a law,  $p = \frac{c}{n^2}$  $\frac{v}{v^2}$ , where C is a constant. **Calculate the work done by the fluid on the piston.**

**Solution. Refer to Fig.1.15.**



**Fig 1.15. Example 1.8**

$$
p_1 = 3bar = 3 \times 10^5 N/m^2
$$
  

$$
v_1 = 0.18m^3/kg
$$

Work done =shaded area= $\int_1^2 p dv$ 

i.e, work done,  $W = \int_{1}^{2} \frac{c}{v^2} dv = C \int_{1}^{2} \frac{dv}{v^2} = C \Big|_{-2+1}^{v^{-2+1}}$  $\frac{1}{-2+1}$  $v_1$ 2 dv  $\int |v^{-2+1}|^{v_2}$  $\mathbf{1}$  $\overline{c}$  $\mathbf{1}$ 

$$
= C[-v^{-1}]_{v_1}^{v_2} = C\left[-\frac{1}{v}\right]_{v_1}^{v_2} = C\left[\frac{1}{v_1} - \frac{1}{v_2}\right] \quad (i)
$$

Also  $C = pv^2 = p_1v_1^2 = 3 \times 10^5 \times 0.18^2 = 0.0972 \times 10^5$ 

Substituting the values of C,  $v_1$  and  $v_2$  in eqn  $\cdot$  (i). we get

$$
v_2^2 = \frac{c}{p} = \frac{0.0972 \times 10^5}{3 \times 10^5} = 0.0324
$$

**Or,**  $v_2 = 0.18 m^3$ 

Work done,  $W = 0.0972 \times 10^5 \Big[ \frac{1}{0.15} \Big]$  $\left[\frac{1}{0.18}-\frac{1}{0.402}\right]=29840\frac{J}{kg}$  $W = 29 \cdot 840 \, kJ/kg$  (Ans.)