

YUNUS A. ÇENGEL and JOHN M. CIMBALA,  
"Fluid Mechanics: Fundamentals and  
Applications", 1<sup>st</sup> ed., McGraw-Hill, 2006.

**Course name**

***Incompressible Fluid Mechanics***

# **Lecture-01 - Chapter-04**

## **Dimensional Analysis And Dynamic Similarity**

Lecture slides by

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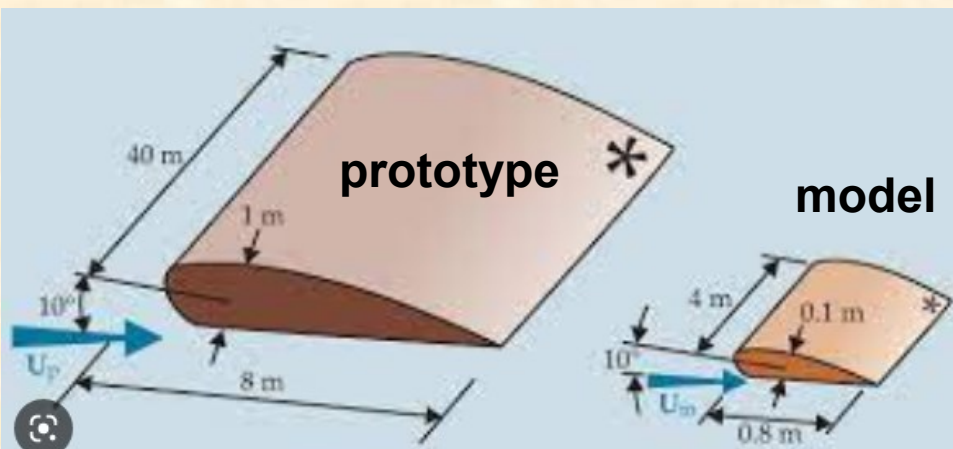
# Outline

- ***Fluid Basics: Introduction***
- ***Dimensions and Units***
- ***Buckingham  $\pi$ - Theorem or PI Theorem***
- ✓ ***Solution Procedure steps***
- ✓ ***Explanatory question***
- ***Nondimensional Parameters***
- ***Examples***
- ***Homeworks***

# Fluid Basics: Introduction

The main principles of **chapter 4** (**chapter 7 in the fluid book**) are:

- Review the concepts of **dimensions and units**.
- Identify dimensionless groups **PI-Theorem**. (**Buckingham**)
- Discuss the concept of similarity between a **model and a prototype**.

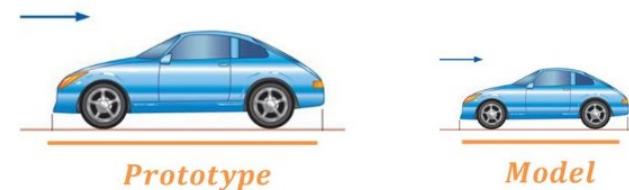


## Dimensional Analysis

How many seconds are in one day?

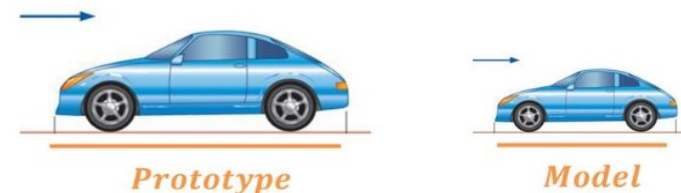
$$\frac{24 \text{ hr}}{1 \text{ day}} \cdot \frac{60 \text{ min}}{1 \text{ hr}} \cdot \frac{60 \text{ s}}{1 \text{ min}} = \frac{\text{s}}{\text{day}} = 86,400 \text{ s/day}$$

## Dimensional Analysis



- Let's say we want to find the drag force on a prototype sports car
- It would be easier to measure the drag on a smaller model and then scale it up

## Dynamic Similarity



- In *dynamic similarity* all of the forces in the smaller flow scale by a constant factor to forces in the larger flow
- For the model and prototype to be *dynamically similar*, **all  $\Pi$  groups must be the same**

• [https://www.youtube.com/watch?v=d\\_WfCwJW0Og](https://www.youtube.com/watch?v=d_WfCwJW0Og)

• <https://slideplayer.com/slide/16883552/>

# 1- Dimensions and Units

<https://www.slideshare.net/YusriYusup/1-dimensions-and-units>

## DIMENSIONS AND UNITS

### Definition:

**Dimensions** are basic concepts of physical measurements such as:

- Length = [L]
- Time = [T]
- Mass = [M]
- Temperature = [θ]

**Units** are terms that precede and describe the dimensions.

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Commonly used derived terms

Derived Term	SI unit	Dimension
Area	m <sup>2</sup>	[L <sup>2</sup> ]
Volume	m <sup>3</sup>	[L <sup>3</sup> ]
Velocity	m/s	[LT <sup>-1</sup> ]
Acceleration	m/s <sup>2</sup>	[LT <sup>-2</sup> ]
Force	N or kgm/s <sup>2</sup>	[MLT <sup>-2</sup> ]
Pressure (stress)	N/m <sup>2</sup> or Pa	[ML <sup>-1</sup> T <sup>-2</sup> ]
Energy (work)	Nm = J (joule)	[ML <sup>2</sup> T <sup>-2</sup> ]
Power	J/s = watt	[ML <sup>2</sup> T <sup>-3</sup> ]

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BASICS OF FLUID MECHANICS

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FLUID MECHANICS

<https://www.youtube.com/watch?v=MLXVistNQyE>

<https://analytics.rowsandall.com/2017/12/02/lets-discuss-rowing-metrics/>

The dimensions of mechanics are force, length, mass and Time. They are related to Newton's 2<sup>nd</sup> law of motion

$$F = m \cdot a \Rightarrow F = mLT^{-2} \Rightarrow \text{نظام ايجاد المقادير من دون افعال لذي تقدير على اجزيات}$$

where

m = mass (kg)

a = acceleration m/s<sup>2</sup>

F = Force (N)

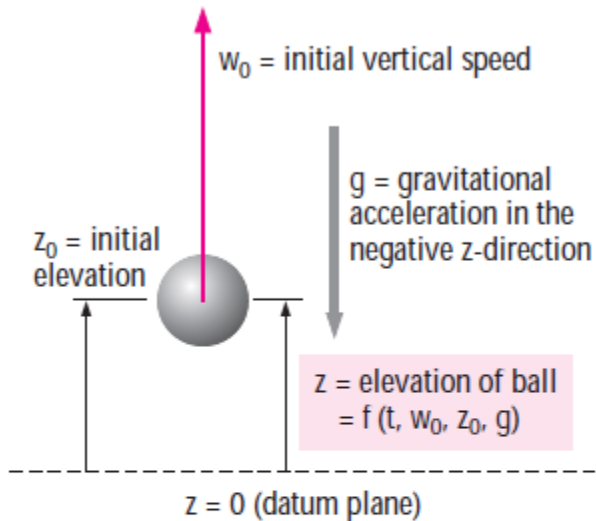
m = mass  
L = Length  
T = Time  
N = force

Physical quantity measured	Base unit	SI abbreviation
	mole	mol
	meter	m
	kilogram	kg
	second	s
	kelvin	K
	ampere	A
	candela	cd

# 2- Buckingham $\pi$ - Theorem or PI Theorem

There are several methods to learn how to generate the non-dimensional parameters, that have been developed for this purpose, but the most popular (and simplest) method is the **method of repeating variables** or **PI-Theorem**, popularized by Edgar Buckingham (1867–1940).

➤ As a simple example, consider a ball falling in a vacuum as discussed in **Section 7–23**.



**FIGURE 7–23**

Setup for dimensional analysis of a ball falling in a vacuum. Elevation  $z$  is a function of time  $t$ , initial vertical speed  $w_0$ , initial elevation  $z_0$ , and gravitational constant  $g$ .

➤ **Basic Dimensions of Common Parameters that are used in  $\pi$ -Theorem**

Quantity	Basic Dimensions	
	FLT System (US)	MLT System (SI)
Acceleration	$LT^{-2}$	$LT^{-2}$
Angular Velocity	$T^{-1}$	$T^{-1}$
Area	$L^2$	$L^2$
Mass Density	$FL^{-4}T^2$	$ML^{-3}$
Weight Density	$FL^{-3}$	$ML^{-2}T^{-2}$
Force (weight)	$F$	$MLT^{-2}$
Kinematic Viscosity	$L^2T^{-1}$	$L^2T^{-1}$
Length	$L$	$L$
Mass	$FL^{-1}T^2$	$M$
Power	$FLT^{-1}$	$ML^2T^{-3}$
Pressure	$FL^{-2}$	$ML^{-1}T^{-2}$
Surface Tension	$FL^{-1}$	$MT^{-2}$
Velocity	$LT^{-1}$	$LT^{-1}$
Viscosity	$FL^{-2}T$	$ML^{-1}T^{-1}$
Volume	$L^3$	$L^3$
Volume Flowrate	$L^3T^{-1}$	$L^3T^{-1}$
Work, Energy	$FL$	$ML^2T^{-2}$

[https://www.ecourses.ou.edu/cgi-bin/eBook.cgi?doc=&topic=fl&chap\\_s ec=06.1&page=theory](https://www.ecourses.ou.edu/cgi-bin/eBook.cgi?doc=&topic=fl&chap_s ec=06.1&page=theory)

# 2- π- Theorem or PI Theorem: Solution Procedure steps

٣- يتم اختيار المتغيرات المذكورة من المتغيرات أعلاه وفق ما يلي :-  
 ١- يجب أن تحتوي الأبعاد MLT مجتمعة مثل  $P, V, D$   
 ٢- عدم اختيار المتغير المطلوب نسبة إلى الأخرى من ضمنها  
 ٣- أن لا يكون أحدها مشتقة الأخرى (السرعة والتسارع)  
 ٤- يفضل اختيار المتغيرات ذات الأبعاد الثنائية أو المفردة  
 ٥- إذا كان هناك أكثر من متغير ذو أبعاد متناسبة تختار أحدها ضمن المتكررة.  
 ٦- عدد المعادلات (πs) تساوي عدد المتغيرات مطروحا منها عدد الأبعاد المتكررة

عدد الأبعاد =  $M$   
 عدد المتغيرات =  $n$   
 $n - M = \text{No. of } \pi_s$

The Buckingham π-Theorem proves that, in a physical problem including  $n$  quantities in which there are  $m$  dimensions. The quantities can be arranged into  $n - m$  groups.

$M$ : عدد الأبعاد وبعده عامة يكون عددها  $M$   
 $n$ : يجب أن لا يقل عن  $M$

لتحديد العلاقات المطلوبة من خلال المتغيرات نستطيع ما يلي

١- يتم اختيار المتغيرات من خلال متطوق التوك  
 ٢- تكتب المتغيرات بعينه الدالة كما يلي  $(P, V, D, \rho, \mu, g, H)$

Number of dimensionless constants = (Number of variables) – (number of fundamental units involved)

## Example:

See examples in the table below:

Given set of variables Constants	Number of variables Constants	Number of fundamental units constants	Number of dimensionless
$l, g, t$	3	2 (L, T)	3 - 2 = 1
$l, v, g$	3	2 (L, T)	3 - 2 = 1
$p, D, \rho, Q$	4	3 (L, M, T)	4 - 3 = 1
$F, D, v, \rho, \mu$	5	3 (L, M, T)	5 - 3 = 2
$Q, H, g, \gamma$	4	2 (L, T)	4 - 2 = 2
$D, N, \mu, p, R$	5	3 (L, M, T)	5 - 3 = 2
$l, v, \rho, \mu, g, R$	6	3 (L, M, T)	6 - 3 = 3
$\Delta p, D, l, \rho, \mu, v, t$	7	3 (L, M, T)	7 - 3 = 4
$l, v, \rho, \mu, E, R$	6	3 (L, M, T)	6 - 3 = 3

(iv) The repeating variables, each raised to an index, are grouped with a non-repeating variable to form a dimensionless constant. For example, if the given variables are  $F, D, v, \rho, g, \mu$  then since there are 6 variables involving 3 fundamental units, we can frame  $6 - 3 = 3$  dimensionless constants. Since three fundamental units are involved we should select three repeating variables. Obviously, the best choice of repeating variables will be  $D, v$  and  $\rho$ .

The three dimensionless constants are given by –

$$\pi_1 = D^{a_1} v^{b_1} \rho^{c_1} F, \pi_2 = D^{a_2} v^{b_2} \rho^{c_2} g$$

and

$$\pi_3 = D^{a_3} v^{b_3} \rho^{c_3} \mu.$$

<https://www.engineeringenotes.com/fluids/dimensional-analysis/dimensional-analysis-of-a-fluid-methods-equations-buckingham-pi-theorem-and-table/47411>

# 2- π- Theorem or PI Theorem: Solution Procedure steps

٥- تكتب المعادلات كما يلي

$$\begin{matrix} x_1 & y_1 & z_1 & 1 \\ \bar{\pi}_1 = & V & D & P & M \\ x_2 & y_2 & z_2 & 1 \\ \bar{\pi}_2 = & V & D & P & C \\ \vdots & \vdots & \vdots & \vdots & \vdots \end{matrix}$$

حيث  $z$  ظافات المتغيرات المستقلة وترفع للأس  $(z, y, x)$   
 أما المتكرره ترفع للأس

٦- أيجاد قيم الأس بعد تعويض أبعاد كل متغير

٧- إيجاد كتايه المعادلات بعد تعويض قيم الأس ثم تكتب  
 كتايه المعادلات بصيغه الدالة

$$f_1(\pi_1, \pi_2, \pi_3, \dots) = 0$$

٨- اذ يكتب المطلوب فمثلاً اذا كان المطلوب قيمه المعادله  
 الادخله  $\pi_1$  بالصيغه التاليه

$$\pi_1 = f_2(\pi_2, \pi_3, \dots)$$

## Example:

### The simple pendulum [edit]

We wish to determine the period  $T$  of small oscillations in a simple pendulum. It will be assumed that it is a function of the length  $L$ , the mass  $M$ , and the acceleration due to gravity on the surface of the Earth  $g$ , which has dimensions of length divided by time squared. The model is of the form

$$f(T, M, L, g) = 0.$$

(Note that it is written as a relation, not as a function:  $T$  isn't written here as a function of  $M$ ,  $L$ , and  $g$ .)

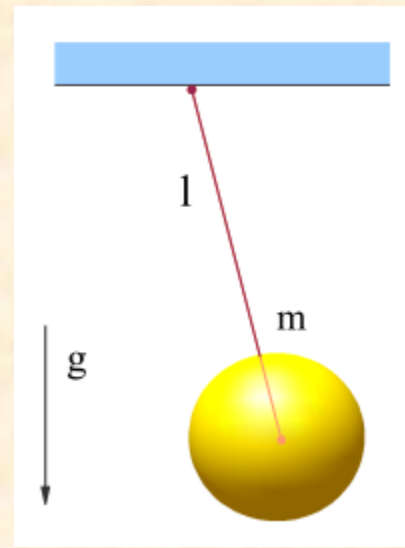
There are 3 fundamental physical dimensions in this equation: time  $t$ , mass  $m$ , and length  $\ell$ , and 4 dimensional variables,  $T$ ,  $M$ ,  $L$ , and  $g$ . Thus we need only  $4 - 3 = 1$  dimensionless parameter, denoted  $\pi$ , and the model can be re-expressed as

$$f(\pi) = 0,$$

where  $\pi$  is given by

$$\pi = T^{a_1} M^{a_2} L^{a_3} g^{a_4}$$

$$\begin{aligned} \pi &= T^2 M^0 L^{-1} g^1 \\ &= gT^2 / L \end{aligned}$$



[https://en.wikipedia.org/wiki/Buckingham\\_pi\\_theorem](https://en.wikipedia.org/wiki/Buckingham_pi_theorem)

# Nondimensional Parameters

## Dimensionless Parameters $f_i = r \frac{V^2}{l}$

- Reynolds Number  $Re = \frac{rVl}{m} \quad f_u = m \frac{V}{l^2}$
  - Froude Number  $Fr = \frac{V}{\sqrt{gl}} \quad f_g = r g$
  - Weber Number  $W = \frac{V^2 l \rho}{\sigma} \quad f_s = \frac{S}{l^2}$
  - Mach Number  $M = \frac{V}{c} \quad f_{E_v} = \frac{r c^2}{l}$
  - Pressure/Drag Coefficients  $C_p = \frac{-2(Dp)}{rV^2} \quad C_d = \frac{2\text{Drag}}{\rho V^2 A}$
- (dependent parameters that we measure experimentally)

Drag coefficient	$C_D = \frac{F_D}{\frac{1}{2}\rho V^2 A}$	$\frac{\text{Drag force}}{\text{Dynamic force}}$
Eckert number	$Ec = \frac{V^2}{c_p T}$	$\frac{\text{Kinetic energy}}{\text{Enthalpy}}$
Euler number	$Eu = \frac{\Delta P}{\rho V^2}$ (sometimes $\frac{\Delta P}{\frac{1}{2}\rho V^2}$ )	$\frac{\text{Pressure difference}}{\text{Dynamic pressure}}$
Fanning friction factor	$C_f = \frac{2\tau_w}{\rho V^2}$	$\frac{\text{Wall friction force}}{\text{Inertial force}}$
Fourier number	$Fo$ (sometimes $\tau$ ) = $\frac{\alpha t}{L^2}$	$\frac{\text{Physical time}}{\text{Thermal diffusion time}}$
Froude number	$Fr = \frac{V}{\sqrt{gL}}$ (sometimes $\frac{V^2}{gL}$ )	$\frac{\text{Inertial force}}{\text{Gravitational force}}$
Grashof number	$Gr = \frac{g\beta \Delta T L^3\rho^2}{\mu^2}$	$\frac{\text{Buoyancy force}}{\text{Viscous force}}$
Jakob number	$Ja = \frac{c_p(T - T_{sat})}{h_{fg}}$	$\frac{\text{Sensible energy}}{\text{Latent energy}}$
Knudsen number	$Kn = \frac{\lambda}{L}$	$\frac{\text{Mean free path length}}{\text{Characteristic length}}$

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- <https://www.slideserve.com/joy/dimensional-analysis-and-similitude>
- <https://www.slideshare.net/ADDISUDAGNEZEGEYE/fluid-mechanics-chapter-5-dimensional-analysis-and-similitude>

**Note:** Just for briefing, you can See table 7–5 in the fluid mechanics book (pp.287-288) that shows some nondimensional parameters.



## 2- $\pi$ - Theorem or PI Theorem: *Explanatory question*

The elevation  $z$  of the ball must be a function of time  $t$ , initial vertical speed  $w_0$ , initial elevation  $z_0$ , and gravitational constant  $g$  (Fig. 7-23).

**Solution:** List of relevant parameters:  $z = f(t, w_0, z_0, g)$   $n = 5$

$z$	$t$	$w_0$	$z_0$	$g$
$\{L^1\}$	$\{t^1\}$	$\{L^1t^{-1}\}$	$\{L^1\}$	$\{L^1t^{-2}\}$

$$n=5 \text{ \& } m=2 : \quad \pi_s = n-m=5-2=3$$

Repeating parameters:  $w_0$  and  $z_0$

Dependent  $\Pi$ :  $\Pi_1 = zw_0^{a_1}z_0^{b_1}$  (7-15)

Dimensions of  $\Pi_1$ :  $\{\Pi_1\} = \{L^0t^0\} = \{zw_0^{a_1}z_0^{b_1}\} = \{L^1(L^1t^{-1})^{a_1}L^{b_1}\}$

Time:  $\{t^0\} = \{t^{-a_1}\}$   $0 = -a_1$   $a_1 = 0$

Length:  $\{L^0\} = \{L^1L^{a_1}L^{b_1}\}$   $0 = 1 + a_1 + b_1$   $b_1 = -1 - a_1$   $b_1 = -1$

Equation 7-15 thus becomes

$$\Pi_1 = \frac{z}{z_0} \quad (7-16)$$

First independent  $\Pi$ :  $\Pi_2 = tw_0^{a_2}z_0^{b_2}$

Dimensions of  $\Pi_2$ :  $\{\Pi_2\} = \{L^0t^0\} = \{tw_0^{a_2}z_0^{b_2}\} = \{t(L^1t^{-1})^{a_2}L^{b_2}\}$

Equating exponents,

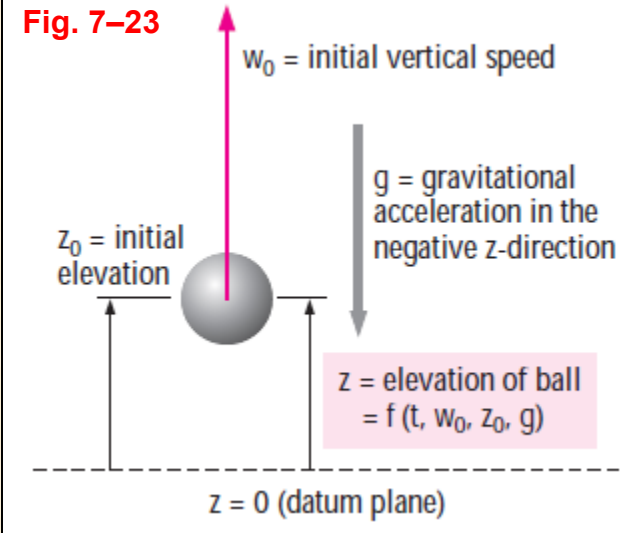
Time:  $\{t^0\} = \{t^{1-a_2}\}$   $0 = 1 - a_2$   $a_2 = 1$

Length:  $\{L^0\} = \{L^{a_2}L^{b_2}\}$   $0 = a_2 + b_2$   $b_2 = -a_2$   $b_2 = -1$

$\Pi_2$  is thus

$$\Pi_2 = \frac{w_0 t}{z_0} \quad (7-17)$$

Fig. 7-23



## 2- $\pi$ - Theorem or PI Theorem: *Explanatory question*

Finally we create the second independent  $\Pi$  ( $\Pi_3$ ) by combining the repeating parameters with  $g$  and forcing the  $\Pi$  to be dimensionless (Fig. 7-26).

$$\text{Second independent } \Pi: \quad \Pi_3 = gw_0^{a_3}z_0^{b_3}$$

$$\text{Dimensions of } \Pi_3: \quad \{\Pi_3\} = \{L^0t^0\} = \{gw_0^{a_3}z_0^{b_3}\} = \{L^1t^{-2}(L^1t^{-1})^{a_3}L^{b_3}\}$$

Equating exponents,

$$\text{Time:} \quad \{t^0\} = \{t^{-2}t^{-a_3}\} \quad 0 = -2 - a_3 \quad a_3 = -2$$

$$\text{Length:} \quad \{L^0\} = \{L^1L^{a_3}L^{b_3}\} \quad 0 = 1 + a_3 + b_3 \quad b_3 = -1 - a_3 \quad b_3 = 1$$

$\Pi_3$  is thus

$$\Pi_3 = \frac{gz_0}{w_0^2} \quad (7-18)$$

$$\text{Modified } \Pi_3: \quad \Pi_{3, \text{modified}} = \left(\frac{gz_0}{w_0^2}\right)^{-1/2} = \frac{w_0}{\sqrt{gz_0}} = Fr \quad (7-19)$$

$$\text{Relationship between } \Pi\text{'s:} \quad \Pi_1 = f(\Pi_2, \Pi_3) \quad \rightarrow \quad \frac{z}{z_0} = f\left(\frac{w_0 t}{z_0}, \frac{w_0}{\sqrt{gz_0}}\right)$$

Or, in terms of the nondimensional variables  $z^*$  and  $t^*$  defined previously by Eq. 7-6 and the definition of the Froude number,

$$\text{Final result of dimensional analysis:} \quad z^* = f(t^*, Fr) \quad (7-20)$$

$$\text{Nondimensionalized variables:} \quad z^* = \frac{z}{z_0} \quad t^* = \frac{w_0 t}{z_0} \quad (7-6)$$

## 2- $\pi$ - Theorem or PI Theorem: *Explanatory question*

**Example:** Flow in a Circular Pipe For a better illustration of the use of dimensional analysis, take fluid flow in a circular pipe.

**Solution:**  $n=7$  &  $m=3$  :  $\pi_s = n-m=7-3=4$

The pi terms are then given by:

$$\Pi_1 = \Delta p D^{a_1} V^{b_1} \rho^{c_1}$$

$$\Pi_2 = l D^{a_2} V^{b_2} \rho^{c_2}$$

$$\Pi_3 = \mu D^{a_3} V^{b_3} \rho^{c_3}$$

$$\Pi_4 = \varepsilon D^{a_4} V^{b_4} \rho^{c_4}$$

The exponents of the first pi terms are determined as follows:

$$\begin{aligned} \Pi_1 = \Delta p D^{a_1} V^{b_1} \rho^{c_1} &= (ML^{-1}T^{-2})(L)^{a_1}(LT^{-1})^{b_1}(ML^{-3})^{c_1} \\ &= M^{(1+c_1)} L^{(-1+a_1+b_1-3c_1)} T^{(-2-b_1)} \end{aligned}$$

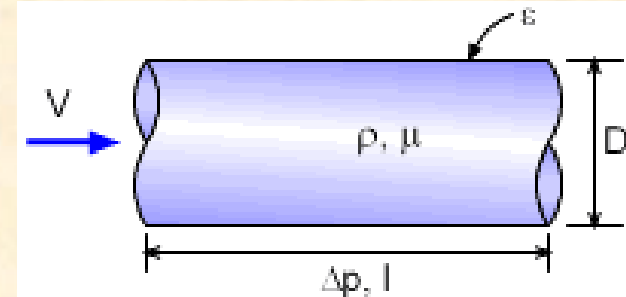
In order for  $\Pi_1$  to be dimensionless:

$$\begin{aligned} M: \quad 1 + c_1 &= 0 \\ c_1 &= -1 \end{aligned}$$

$$\begin{aligned} T: \quad -2 - b_1 &= 0 \\ b_1 &= -2 \end{aligned}$$

$$\begin{aligned} L: \quad -1 + a_1 + b_1 - 3c_1 &= 0 \\ a_1 &= 3(-1) - (-2) + 1 = 0 \end{aligned}$$

Hence,  $\Pi_1$  is determined to be  $\Delta p / \rho V^2$ .



Fluid Flow in a Circular Pipe

Quantity	Symbol	MLT
Pressure Drop	$\Delta p$	$ML^{-1}T^{-2}$
Pipe Length	$l$	$L$
Pipe Diameter	$D$	$L$
Fluid Velocity	$V$	$LT^{-1}$
Fluid Density	$\rho$	$ML^{-3}$
Fluid Viscosity	$\mu$	$ML^{-1}T^{-1}$
Pipe Surface Roughness	$\varepsilon$	$L$

[https://www.ecourses.ou.edu/cgi-bin/eBook.cgi?doc=&topic=fl&chap\\_sec=06.1&page=theory](https://www.ecourses.ou.edu/cgi-bin/eBook.cgi?doc=&topic=fl&chap_sec=06.1&page=theory)

## 2- $\pi$ - Theorem or PI Theorem: *Explanatory question*

Since the basic dimension for the pipe length  $l$  is  $L$ , by inspection, the second pi term is given by ( $a_2 = -1$ ,  $b_2 = 0$  and  $c_2 = 0$ ):

$$\Pi_2 = l/D$$

Similarly, the last pi term is given by ( $a_4 = -1$ ,  $b_4 = 0$  and  $c_4 = 0$ ):

$$\Pi_4 = \varepsilon/D$$

The exponents of the third pi terms are determined as follows:

$$\begin{aligned}\Pi_3 &= \mu D^{a_3} V^{b_3} \rho^{c_3} = (ML^{-1}T^{-1})(L)^{a_3}(LT^{-1})^{b_3}(ML^{-3})^{c_3} \\ &= M^{(1+c_3)} L^{(-1+a_3+b_3-3c_3)} T^{(-1-b_3)}\end{aligned}$$

In order for  $\Pi_3$  to be dimensionless:

$$\begin{aligned}M: \quad &1 + c_3 = 0 \\ &c_3 = -1\end{aligned}$$

$$\begin{aligned}T: \quad &-1 - b_3 = 0 \\ &b_3 = -1\end{aligned}$$

$$\begin{aligned}L: \quad &-1 + a_3 + b_3 - 3c_3 = 0 \\ &a_3 = 3(-1) - (-1) + 1 = -1\end{aligned}$$

Hence,  $\Pi_3$  is determined to be  $\mu/\rho DV$ . Recognizing that the inverse of the pi term is also dimensionless, the third pi term can also be written as  $\rho DV/\mu$ , which is the [Reynolds number \(Re\)](#).

For flow in a circular pipe, the pressure drop is then given by

$$\Delta p/\rho V^2 = \text{function}(l/D, \varepsilon/D, Re)$$

[https://www.ecourses.ou.edu/cgi-bin/eBook.cgi?doc=&topic=fl&chap\\_sec=06.1&page=theory](https://www.ecourses.ou.edu/cgi-bin/eBook.cgi?doc=&topic=fl&chap_sec=06.1&page=theory)

# Examples

## Example<sub>1</sub>: Primary Dimensions of Surface Tension

An engineer is studying how some insects are able to walk on water (Fig.7–2). A fluid property of importance in this problem is surface tension ( $\sigma_s$ ), which has dimensions of force per unit length. Write the dimensions of surface tension in terms of primary dimensions.

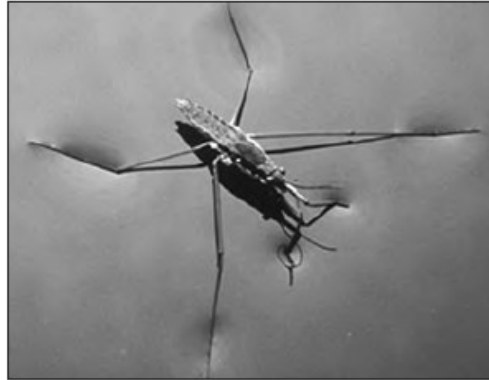


FIGURE 7–2

The water strider is an insect that can walk on water due to surface tension.

© Dennis Drenner/Visuals Unlimited.

**SOLUTION** The primary dimensions of surface tension are to be determined.

**Analysis** From Eq. 7–1, force has dimensions of mass times acceleration, or  $\{mL/t^2\}$ . Thus,

$$\text{Dimensions of surface tension: } \{\sigma_s\} = \left\{ \frac{\text{Force}}{\text{Length}} \right\} = \left\{ \frac{m \cdot L/t^2}{L} \right\} = \{m/t^2\} \quad (1)$$

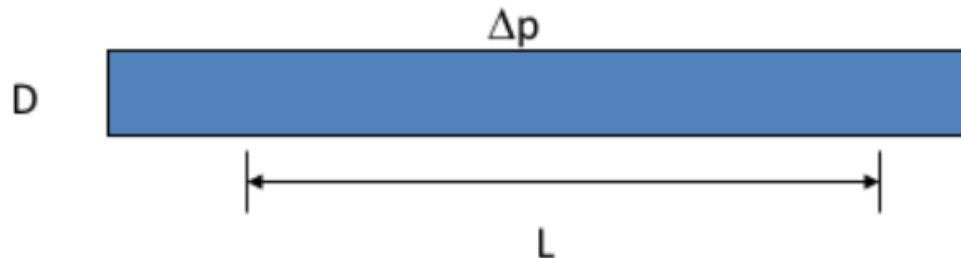
**Where:**

$$\text{Dimensions of force: } \{\text{Force}\} = \left\{ \text{Mass} \frac{\text{Length}}{\text{Time}^2} \right\} = \{mL/t^2\} \quad (7-1)$$

# Homeworks:

**HW1:** Using Buckingham Pi theorem, determine the dimensionless P parameters involved in the problem of determining pressure drop along a straight horizontal circular pipe shown below. The relevant flow parameters are:

- $\Delta p$  pressure drop,
- $\rho$  density,
- $V$  averaged velocity,
- $\mu$  viscosity
- $L$  pipe length
- $D$  pipe diameter.



Hint: Use the following product groups:

- Group 1 :  $\rho, V, D, \Delta p$
- Group 2 :  $\rho, V, D, \mu$
- Group 3:  $\rho, V, D, L$

➤ Note:

- Solve all five Homeworks and sending me the answering next week on Sunday 21 March 2024.
- Read examples 7-7 & 7-8 in the fluid mechanics book (pp.290-293)

□ I hope everything is clear for all students

❖ Good luck